

Maxwell equation in differential and integral form  $\rightarrow$

1.  $\nabla \cdot \vec{D} = \rho$ ,  $\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$  Gauss law of electrostatics here  $D = \epsilon_0 E$

$D =$  Displacement density and

$\rho =$  volume charge density

Integral form  $\rightarrow$

$$\nabla \cdot \vec{D} = \rho$$

Taking volume integral

$$\int_V \nabla \cdot \vec{D} dV = \int_V \rho dV$$

by Gauss divergence theorem

$\int_V \nabla \cdot \vec{D} dV$  can be written as -

$$\int_S \vec{D} \cdot d\vec{s}$$

Sunday 5

$$\boxed{\int_S \vec{D} \cdot d\vec{s} = \int_V \rho dV = q}$$

2)  $\nabla \cdot \vec{B} = 0$  Gauss law for magnetostatic here

2010	AUGUST					2010	SEPTEMBER
Mon	30	2	9	16	23	Mon	6
Tue	31	3	10	17	24	Tue	7
Wed		4	11	18	25	Wed	8
Thu		5	12	19	26	Thu	9
Fri		6	13	20	27	Fri	10
Sat		7	14	21	28	Sat	11
Sun		1	8	15	22	Sun	12



$B =$  Magnetic field / M.F density

Integral form  $\rightarrow$

$$\vec{\nabla} \cdot B = 0$$

Taking volume integral

$$\int_V \vec{\nabla} \cdot B dV = 0$$

By Gauss divergence theorem

$$\int_S B \cdot ds = 0$$

we have  $B = \mu_0 H$

$$\int_S \mu_0 H ds = 0$$

$$\boxed{\int_S H ds = 0}$$

$$3) \vec{\nabla} \times E = - \frac{\partial B}{\partial t}$$

Faradays law of

electromagnetic here

$E =$  Electric field intensity

Integral Form  $\rightarrow$

$$\vec{\nabla} \times E = - \frac{\partial B}{\partial t}$$

Integrating over surface  $S$

	OCTOBER	2010	NOVEMBER
4	11 18 25	Mon	1 8 15 22 29
5	12 19 26	Tue	2 9 16 23 30
6	13 20 27	Wed	3 10 17 24
7	14 21 28	Thu	4 11 18 25
8	15 22 29	Fri	5 12 19 26
2	9 16 23 30	Sat	6 13 20 27
3	10 17 24		



$$\int_S (\vec{\nabla} \times \vec{E}) \cdot d\vec{s} = - \int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{s}$$

By Stoke's theorem

$\int_S (\vec{\nabla} \times \vec{E}) \cdot d\vec{s}$  can be written as

$$\oint E \cdot dl$$

$$\oint E \cdot dl = - \frac{\partial}{\partial t} \int_S \vec{B} \cdot d\vec{s}$$

4)  $\vec{\nabla} \times H = \vec{J} + \frac{\partial \vec{D}}{\partial t}$  Modified amp.  
circuital here

$H = M \cdot F$  intensity

$\vec{J} =$  current density

and  $\frac{\partial \vec{D}}{\partial t} =$  Displacement current density

Integral form  $\rightarrow$

$$\vec{\nabla} \times H = \int \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

Integrating over surface  $S$ .

2010	AUGUST					2010	SEPTEMBER
Mon	30	2	9	16	23	Mon	6 13 20 27
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Wed		4	11	18	25	Wed	1 8 15 22 29
Thu		5	12	19	26	Thu	2 9 16 23 30
Fri		6	13	20	27	Fri	3 10 17 24
Sat		7	14	21	28	Sat	4 11 18 25
Sun		1	8	15	22	Sun	5 12 19 26

$$\int_S (\vec{\nabla} \times \mathbf{H}) \, d\mathbf{s} = \int_S \left( \vec{\mathbf{J}} + \frac{\partial \mathbf{D}}{\partial t} \right) d\mathbf{s}$$

By Stokes theorem

$$\oint \mathbf{H} \cdot d\mathbf{l} = \int_S \left( \vec{\mathbf{J}} + \frac{\partial \vec{\mathbf{D}}}{\partial t} \right) d\mathbf{s}$$

we know  $\mathbf{B} = \mu_0 \mathbf{H}$

$$\oint \mathbf{B} \cdot d\mathbf{l} = \mu_0 \int_S \left( \vec{\mathbf{J}} + \frac{\partial \vec{\mathbf{D}}}{\partial t} \right) d\mathbf{s}$$

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